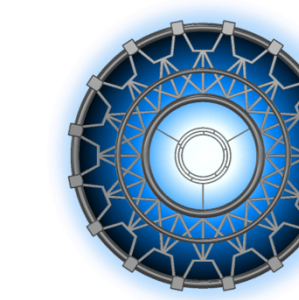


STOCHASTIC RESOURCE OPTIMIZATION OVER HETEROGENEOUS GRAPH NEURAL NETWORKS FOR FAILURE-PREDICTIVE MAINTENANCE SCHEDULING

ZHEYUAN WANG*, MATTHEW GOMBOLAY*

*CORE Robotics Lab, School of Interactive Computing, Georgia Institute of Technology, Atlanta, GA, USA

<https://core-robotics.gatech.edu/> E-mail: {pjohngwang,mgombolay3}@gatech.edu



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Motivation

- Resource optimization for predictive maintenance requires inferring and **reasoning over stochastic failure models** and dynamically allocating repair resources.
- Predictive maintenance scheduling is typically performed with ad hoc, hand-crafted heuristics and manual scheduling by human experts, which is **time-consuming, laborious** and **hard to scale**.
- Recent **advances in AI** have leveraged deep neural networks to solve operations research problems, but **only touched** static, deterministic setting.

Aircraft Maintenance Environment

- AirME (hour-based discrete time system)
 - Heterogeneous aircraft, $\{p_i\}$
 - Homogeneous maintenance crews, $\{c_j\}$
 - A maintenance decision, $d = \langle p_i, c_j \rangle$
- Hybrid probabilistic failure model
 - Model component/part failure using **Weibull distributions** based on aircraft usage

$$p(x; \lambda, k) = \frac{k}{\lambda} \left(\frac{x}{\lambda}\right)^{k-1} e^{-(x/\lambda)^k}, x \geq 0$$
 - Model parameters hidden from scheduling policies
- Stochastic** aircraft maintenance task
 - Duration and cost generated on-the-fly
- Sample flying operations based on usage rate
 - Different planes earn different hourly income
- Scheduling objectives
 - O1: overall **profit**; O2: **revenue** only; O3: fleet **availability**
- POMDP formulation

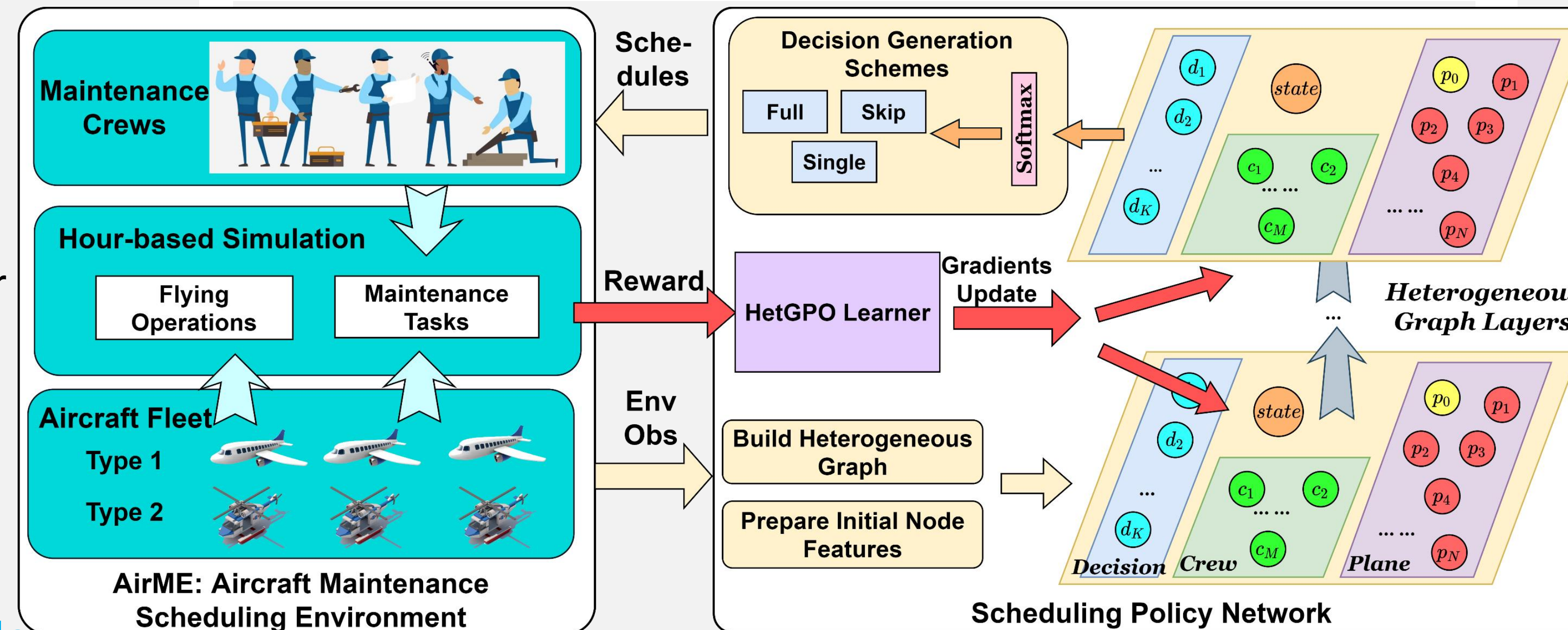


Fig. 1. Overview of AirME and Scheduling Policy Network

Stochastic Scheduling with Graphs

- Scheduling Policy Network, $\pi_\theta(u|o)$
 - Fully graph convolutional structure
 - Action $u_t = \{d_1, d_2, \dots, d_n\}$
 - Conditional policy

$$p_\theta(u_t|o_t) = \prod_{i=1}^n p_\theta(d_i|o_t, d_{1:i-1})$$
 - Decision generation schemes: **Full, Skip, Single**
- Heterogeneous Graph** Representation
 - Joint learning** the problem representation and the policy
 - Model entities in the environment
 - Planes, crews
 - Model RL components
 - State, decisions
- A novel **heterogeneous graph attention layer**
 - Building block of our scheduling policy network
 - Computation Step
 - per-edge-type** message passing
 - per-node-type** feature reduction
 - Uses multi-head attention

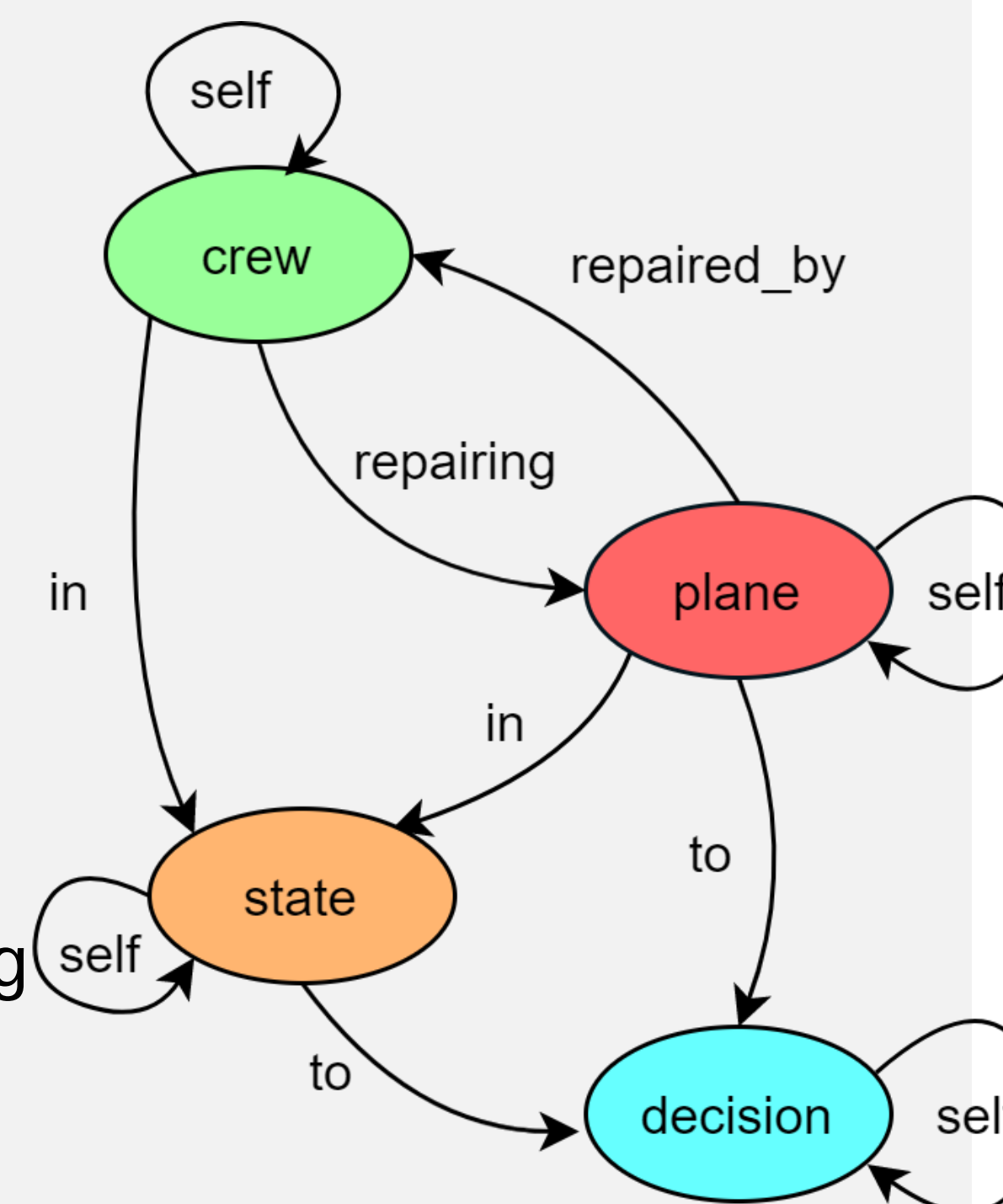


Fig. 2. Metagraph

Heterogeneous Graph-based Policy Optimization

- HetGPO
 - Developed from Proximal Policy Optimization (PPO) with **several adaptations** for stochastic scheduling
- Clipped surrogate objective

$$L(\theta) = E_t[\min(r_t(\theta)A_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon)A_t)]$$

$$r_t(\theta) = \frac{\pi_\theta(u|o)}{\pi_{old}(u|o)} \quad A_t: \text{Advantage term}$$
- Step-based baseline** for variance reduction
- Use idea of **curriculum learning**

Experimental Results

- Benchmark HetGPO against
 - Hand-crafted heuristics, Model-based planning
 - Machine learning-based methods
- Dataset: small, medium and large AirME instances
- Evaluation on O1, O2, O3 using
 - M1: normalized** objective value
 - M2: % improvement** over the Corrective Scheduler
- Ablation studies

Table I. Evaluation results on O1: profit

Methods	Small		Medium		Large	
	M1	M2 (%)	M1	M2 (%)	M1	M2 (%)
Random	0.522 ± 0.025	-2.87 ± 5.65	0.532 ± 0.021	-2.65 ± 4.22	0.533 ± 0.016	-2.23 ± 3.51
Corrective	0.539 ± 0.023	0.0 ± 0.0	0.547 ± 0.016	0.0 ± 0.0	0.546 ± 0.016	0.0 ± 0.0
Condition-based	0.656 ± 0.050	21.7 ± 6.41	0.661 ± 0.041	20.8 ± 5.87	0.648 ± 0.051	18.6 ± 7.03
Periodic	0.599 ± 0.051	11.1 ± 6.96	0.598 ± 0.047	9.38 ± 7.00	0.587 ± 0.048	7.52 ± 6.83
Model-based	0.669 ± 0.052	24.0 ± 6.99	0.671 ± 0.044	22.8 ± 6.45	0.658 ± 0.054	20.5 ± 7.68
DeepRM	0.533 ± 0.015	-0.88 ± 2.57	0.538 ± 0.011	-1.47 ± 1.77	0.539 ± 0.013	-1.11 ± 0.97
Decima	0.651 ± 0.021	21.1 ± 6.42	0.660 ± 0.017	20.9 ± 4.49	0.663 ± 0.014	21.6 ± 4.51
HetGPO-Single	0.680 ± 0.012	26.4 ± 4.32	0.676 ± 0.011	23.7 ± 3.17	0.666 ± 0.011	22.3 ± 3.77
HetGPO-Skip	0.695 ± 0.010	29.1 ± 4.09	0.697 ± 0.009	27.5 ± 2.70	0.695 ± 0.008	27.5 ± 2.72
HetGPO-Full	0.693 ± 0.011	28.8 ± 4.01	0.694 ± 0.009	27.1 ± 2.62	0.693 ± 0.008	27.1 ± 2.68

See paper for full results on O2, O3

Conclusion

- HetGPO **outperforms** both heuristics and learning-based counterparts
- Future work involves applying HetGPO to a **broader class** of stochastic resource optimization problems